Estimating deformation demands on steel EBF systems

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ABSTRACT
The deformation capacity of a steel eccentrically braced frame (EBF) structure is typically governed by the chord rotation capacity of the EBF links. Codes allow these chord rotation demands to be estimated a variety of ways, from simplified hand calculations through to advanced non-linear analyses. Recent studies have suggested that the elastic analysis approach recommended by the New Zealand steel industry may be non-conservative. Consequently, this paper compares the deformations predicted by current industry recommendations with the results obtained from non-linear static pushover analyses for a series of multi-storey EBF structures. To better estimate the actual link rotation demands in design, a simplified displacement-based method is also used, identifying three deformation components (links, braces and columns) and their contributions to storey drifts. Through a series of case studies, the deformation-component method is shown to perform well, giving more accurate predictions of the actual displacement profiles and link rotation demands of multi-storey EBF structures compared to the current industry guidelines. Therefore, it is recommended that the industry consider replacing current guidelines for estimation of rotation demands on EBF links with a deformation component approach.

1 INTRODUCTION

1.1 Background
Investigations into the seismic behaviour of eccentrically braced frame (EBF) structures such as that shown in Figure 1, were first began in Japan during the 1970’s (O’Reilly and Sullivan, 2015). An EBF structure is treated as a ductile lateral load resisting system that is desirable for use in regions of high seismicity, as shown in Figure 1. Links are designed to yield under intense shaking, either in shear, flexure or a combination of the two. The hysteretic response of the links dissipates large amounts of energy in comparison to a similar concentrically braced frame configuration (O’Reilly and Sullivan, 2015). Numerous experiments were performed to investigate the seismic behaviour of these links in the 1980’s and demonstrated that well-detailed EBF systems possess good ductility capacity and are capable of sustaining large inelastic deformation demands (Sullivan, 2013).
Seismic assessment of a structural system typically requires consideration of the nonlinear force-displacement response. The current NZS 1170.5:2004 includes provisions for the calculation of deformation demands on EBF structures subject to earthquake loading, with several simplifications. However, such responses can be better estimated from nonlinear static analysis, also referred to as pushover analysis, in which a set of incrementally increasing lateral loads is applied on structures and the internal member forces and deformations are computed at each increment (Sullivan et al., 2018).

A number of computer programs, such as Ruauomoko (Carr, 2007), are now available to permit the application of pushover analysis in practice. However, the modelling process requires a certain level of knowledge in structural dynamics and careful calibration of multiple parameters to obtain the correct result. Therefore, industry will benefit from a simplified method to obtain a relatively accurate estimate of the actual displacement profile and deformation demands on EBF structures.

In light of the above, the objective of this paper is to develop and evaluate the performance of the simplified pushover analysis procedure for steel EBF structures by comparing its results to those obtained from the pushover analysis on computer-based models. A series of case study structures are designed and analysed to illustrate the method’s potential and gauge the likely benefits it offers over the existing guidelines. By applying this simplified mechanics-based method, engineers may gain a better understanding of the key characteristics of EBF structures and may motivate the development of alternative methods for the prediction of deformation demands.

2 METHODOLOGY

2.1 Current code method

The current design code of EBF structures with centrally located links mainly focuses on strength criteria. The detailed seismic design procedure consists of three steps. Firstly, with references to NZS 3404 (NZS 3404, 1997) and NZS 1170.5 (NZS 1170.5, 2004), the base shear value, \( V \), and the ductility demand, \( \mu \), are determined for the structure based on the site location and soil condition. Then the lateral loads are distributed to each level of the frame using the Equivalent Static Method. The structure is analysed under the applied lateral forces, which returns a prediction of the rooftop displacement, \( \Delta_{\text{top}} \).

The Heavy Engineering Research Association (HERA) guidelines indicate that the next step is to assess the deformation demands, or the inelastic rotation angle of the link at each floor. Firstly, the drift demand of the whole structure is calculated using Equation 1, as suggested in NZS 1170.5 (NZS 1170.5, 2004).

\[
\theta_p = \tan^{-1}\left(\frac{(\mu - 1)k_d\Delta_{\text{top}}}{H}\right)
\]

Where \( \theta_p \) is the inelastic storey rotation angle; \( k_d \) is the deflection scale factor; and \( H \) is the total height of the structure. The HERA guidelines assumed that all stories have the same amount of drift demand. The inelastic link rotation, \( \gamma_p \), is then calculated based on geometrical relationships, as shown in Equation 2.

\[
\gamma_p = \frac{L\theta_p}{e}
\]

Where \( L \) is the span; and \( e \) is the length of the link. The active link rotation calculated is assessed against the total deformation limit of 0.08 rad, as suggested in the current code NZS 3404 (NZS 3404, 1997). The storey
drift calculated earlier is also compared with the serviceability criteria specified in NZS 1170.5 (NZS 1170, 2004).

The last design step is to conduct force-based analysis and capacity design to identify the shear force and bending moment demand on each member. The members and connections are then designed to meet these strength criteria.

2.2 Ruaumoko modelling

To estimate the actual displacement profile of EBF structures under lateral loading, a series of structural models of EBF systems were created in Ruaumoko to conduct 2D force-based pushover analysis, with a constant triangle force distribution profile over the building height. Several assumptions were made during this stage to ensure the models created could represent the corresponding EBF structures proposed.

The floor diaphragms were assumed to be rigid, which led to all nodes at the same height above the ground level being constrained in the X-direction displacement. The vertical shear area, \( A_v \), of all links were assumed to be the effective web area calculated using Equation 3.

\[
A_{v,\text{link}} = (d - t_f) t_w
\]

Where \( d \) is the depth of the section; \( t_f \) is the thickness of the flange; and \( t_w \) is the thickness of the web. The links were modelled using a bilinear hysteretic shape, with a post-yield stiffness of 0.05 as suggested by O’Reilly and Sullivan (2015). Their yielding moments were set to be equal to the bending moments on the links corresponding to the development of their shear capacities calculated using Equation 4, to ensure the links fail in shear as expected from the short link assumption.

\[
V_{\text{link},i} = 0.577 F_{y,\text{link},i} A_{v,\text{link},i}
\]

Where \( F_{y,\text{link}} \) is the shear yield stress of the link at level i. The storey drift values obtained from the Ruaumoko output file were later used to calculate the overall displacement profile. The link rotations from the Ruaumoko pushover analysis, \( \gamma_{RMK,\text{link},i} \), were obtained by summing the vertical displacements of the two end nodes of the link and dividing by the length of the link.

2.3 Deformation components method

2.3.1 Criteria to assess yielding

The deformation of EBF structure was assessed by first identifying the storey drifts at yield, \( \theta_{y,i} \), at level i. It was estimated by considering three deformation components, as shown in Equation 5.

\[
\theta_{y,i} = \theta_{\text{link},i} + \theta_{\text{br},i} + \theta_{\text{cols},i}
\]

Where \( \theta_{\text{link},i} \), \( \theta_{\text{br},i} \) and \( \theta_{\text{cols},i} \) represent the contributions from the link (including the beam) rotations, the brace strains and the column strains respectively. At yield, the braced beam could be idealised as being simply supported between the column and the link centre, subject to a point load, \( P \), as shown in Figure 2. The magnitude of the force \( P \) was calculated using Equation 6.

\[
P = 0.577 F_{y,\text{link}} A_v (1 + \frac{e}{L_b - e})
\]

Where \( L_b \) is the frame span; \( F_{y,\text{link}} \) is the link yielding stress; and \( A_v \) is the effective shear area. The link contribution, \( \theta_{\text{link},y,i} \), at level i was calculated from the vertical displacement of the beam-brace joint, \( \delta_{v,i} \), as shown in Equation 7 and Equation 8.
\[ \delta_{v,i} = 0.577F_{y,\text{link},i}A_{v,i}\left(\frac{e_{l}^{2}(h_{b,i}-e_{l})}{2AE_{i}i} + \frac{e_{l}}{2GA_{v,i}}\right) \]  
(7)

\[ \theta_{\text{link},y,i} = \frac{2\delta_{v,i}}{h_{b,i}-e_{l}} \]  
(8)

Where \( E \) is the elastic modulus; \( G \) is the shear modulus; \( I \) is the second moment of inertia of the beam and all the other symbols have been defined earlier. The brace and column components were calculated from the brace strains, \( \varepsilon_{\text{br},i} \), and the column strains, \( \varepsilon_{\text{col},i} \) (obtained as dividing the axial forces acting on them by their cross-sectional area), as shown in Equation 9 and Equation 10.

\[ \theta_{\text{br},y,i} = \frac{2\varepsilon_{\text{br},i}}{\sin(2\alpha_{i})} \]  
(9)

\[ \theta_{\text{col},y,i} = \frac{2\varepsilon_{\text{col},(h_{i}-h_{s,i})}}{L_{b}/2} \]  
(10)

Where \( \alpha_{i} \) is the angle between the brace and the beam; \( h_{i} \) is the height to the top of storey \( i \); and \( h_{s,i} \) is the inter-storey height at level \( i \).

### 2.3.2 Elastic displacement profiles

The storey shear capacity (resistance) at level \( i \), \( V_{R,i} \), was calculated by analysing the force equilibrium when the link was yielding in shear, as shown in Equation 11.

\[ V_{R,i} = V_{\text{link},i}\frac{L_{b}}{h_{s,i}} \]  
(11)

The corresponding bending moment diagram (BMD) and shear force diagram (SFD) of a single storey EBF structure are shown in Figure 3, where \( V_{\text{link},i} \) is the shear capacity of the link at level \( i \) calculated using Equation 4. With the storey shear resistance (Equation 11) and the storey drift at yield (Equation 5) identified, the secant stiffness at level \( i \) until yield, \( k_{y,i} \), could be computed using Equation 12.

\[ k_{y,i} = \frac{V_{R,i}}{\theta_{y,i}h_{s,i}} \]  
(12)

The stiffness values were assumed to be constant within the elastic range. The base shear, \( V_{b} \), was then distributed to each floor as a set of lateral forces, \( F_{i} \), using Equation 13.

\[ F_{i} = \frac{\Delta m_{i}}{\sum \Delta m_{i}} V_{b} \]  
(13)

Where \( \Delta_{i} \) is the proposed displacement value (proportional with height) and \( m_{i} \) is the seismic mass at level \( i \). The elastic displacement profile was then obtained by pushing the structure until the first link yielded under the proposed force distribution. The storey shear demand, \( V_{D,i} \), at that instant was computed by summing up the lateral forces from all the storeys above. The elastic displacement profile of the structure was obtained by accumulating the inter-storey displacements calculated using Equation 14, which were also used to compute the elastic storey drift, as shown in Equation 15.

\[ \Delta_{\text{inter elastic},i} = \frac{V_{D,i}}{k_{y,i}} \]  
(14)

\[ \theta_{\text{elastic},i} = \frac{\Delta_{\text{inter elastic},i}}{h_{s,i}} \]  
(15)

*Figure 3: BMD and SFD of a one storey EBF structure under lateral load*
2.3.3 Post-yield displacement profiles

Since the sway mechanism employed into the design of EBF structures sees the deformation demands spread over the building height, their post-yield displacement shapes were proposed based on the beam sway mechanism in moment resisting frames. According to Sullivan et al. (2018), the total displacement profile is taken by uniformly scaling profile from the elastic displacement profile to the target drift level, as shown in Equation 16.

\[ \theta_{u,i} = k_{t_a} \theta_{\text{elastic},i} \]  

(16)

Where \( \theta_{u,i} \) is the ultimate post-yield storey drift at the target displacement; and \( k_{t_a} \) is a constant scale factor for all stories to obtain that target displacement.

Theoretically, it is assumed that all post-yield deformation in the EBF structure will concentrate at links (O’Reilly and Sullivan, 2015). This means that the values of the drift components from braces and columns at the ultimate displacement profile are the same as those at the storey yielding limit. Therefore, the ultimate link component, \( \theta_{\text{link},u,i} \), was calculated using Equation 17.

\[ \theta_{\text{link},u,i} = \theta_{u,i} - \theta_{\text{br},i} - \theta_{\text{cols},i} \]  

(17)

Once the link drift component was known, the vertical displacement of the beam-brace joint could be calculated by rearranging Equation 8, as shown in Equation 18.

\[ \delta_{v,i} = \theta_{\text{link},u,i} \frac{(L_b - e_i)}{2} \]  

(18)

The ultimate link rotation at level \( i \), \( \gamma_{DCL,\text{link},i} \), was then calculated as shown in Equation 19.

\[ \gamma_{DCL,\text{link},i} = \frac{2 \delta_{v,i}}{e_i} \]  

(19)

Where \( \gamma_{DCL,\text{link},i} \) represents the link rotation demand at the ultimate displacement profile calculated using the deformation components method.

In summary, the deformation components method could be summarised in the flow chart shown in Figure 4.

3 RESULTS AND DISCUSSION

3.1 Preliminary results

As explained in Section 2.2, to evaluate the performance of the deformation components method, a series of EBF structures with different dimensions, section details and number of levels were analysed in Ruaumoko using advanced non-linear pushover analysis. Their displacements at each level and storey drift demands at different limit states are compared with those predicted by the deformation components method in this section.

3.1.1 One storey EBF comparison - Elastic

A series of one storey EBF structures proposed by O’Reilly and Sullivan were analysed (O’Reilly and Sullivan, 2015). Since these structures had only one
storey, the column axial deformations were assumed to be negligible. Therefore, these comparisons could be used to verify whether the link and brace component in the deformation components method were giving accurate predictions.

During the Ruamoko modelling stage, all nodes at the top were constrained in the X-direction displacement considering the rigid floor diaphragm assumption. They were pushed under an incremental lateral load at the top until the link yielded. The shear forces on the links obtained from the Ruamoko output file were used to check whether it reached its elastic shear capacity.

For the deformation components method, as introduced above, the force and the vertical displacement of the link at yield were calculated using Equation 6 and Equation 7 respectively. The yield drift of the EBF structure was determined as the sum of the brace and link components. The column component in this case was equal to zero as $h_i = h_{s,i}$ for all one storey structures. The calculated storey drifts at yield were compared with the Ruamoko results for a total number of 10 cases. The errors between the deformation components method’s predictions and the Ruamoko results were all within 1%. Therefore, the proposed deformation components method has sufficient accuracy in estimating the storey drifts at yield for single storey EBF structures.

3.1.1 Multi-storey EBF comparison

The performance of the deformation components method on multi-storey EBF structures was evaluated using a series of case study buildings consisting of regular 5, 10 and 15 storey EBF systems. The structures used were designed by Sullivan (2013). Static pushover analyses were conducted on their corresponding Ruamoko models and two limit states were identified. The elastic limit state (ELS) was at the first link yielding, and the ultimate limit state (ULS) was at the first appearance of a total link rotation of 0.08 rad, based on the suggestion on link rotation capacities in NZS 3404 (NZS 3404, 1997).

For the 5-storey EBF structure, the ELS appeared at a base shear of 1180.5 kN, calculated from the deformation components method. It was predicted that the link at the first storey yielded at its shear capacity of 261.4 kN, as calculated from Eq. (4), before any other links. The result from the Ruamoko pushover analysis matched this prediction. The ULS was predicted using the deformation components method to occur when the link rotation at Level 3 reached 0.08 rad. However, the Ruamoko model gave a different result, with the link on Level 1 reaching 0.08 rad before any other links. The storey drift values obtained from the two methods were then used to calculate the displacement profiles over the building height. Similar processes were conducted on the 10-storey and 15-storey EBF structures. Their displacement profile comparisons are summarised in Figure 5. The storey drift values at ELS and ULS were also compared, with results summarised in Table 1.

Table 1: Errors in ELS and ULS storey drift predictions, with numbers in brackets indicating the storey at which the error appeared

<table>
<thead>
<tr>
<th>Case Number</th>
<th>5-Storey</th>
<th>10-Storey</th>
<th>15-Storey</th>
</tr>
</thead>
<tbody>
<tr>
<td>ELS-MAX</td>
<td>2.1% (1)</td>
<td>8.9% (8)</td>
<td>23.8% (5)</td>
</tr>
<tr>
<td>ELS-MIN</td>
<td>-44.8% (5)</td>
<td>-71.1% (10)</td>
<td>-97.1% (15)</td>
</tr>
<tr>
<td>ULS-MAX</td>
<td>56.8% (4)</td>
<td>64.6% (7)</td>
<td>31.7% (6)</td>
</tr>
<tr>
<td>ULS-MIN</td>
<td>-15.5% (1)</td>
<td>-56.4% (10)</td>
<td>-96.8% (15)</td>
</tr>
</tbody>
</table>

Where a positive error indicates that the predicted storey drift was higher than the Ruamoko analysis result.
Overall, the performance of the deformation components method was good at predicting the displacement profile at lower stories (< 5), with most of errors less than 5%. At higher levels, the error tended to increase especially at the top two floors. On the contrary, the deformation components method did not predict the storey drift well in the three proposed structures at both ELS and ULS. Large underestimations of storey drifts were commonly seen at higher levels.

After comparing the predicted member forces with those obtained from the Ruaumoko output file, two potential sources of errors were identified. The first one was that the deformation components method tends to underestimate the storey shear at the two limit states. For example, in the 5-storey EBF case, the storey shear force at Level 5 was underestimated by 8% compared to the actual shear force used in Ruaumoko. This was suspected to be the result of the error in the column axial force prediction, which had a greater effect on top stories.

The second source of error came from the storey stiffness estimation. This was caused by the underestimation of the vertical displacement at link ends, $\delta_v$, compared with the Ruaumoko analysis results, which resulted in the storey drift at yield being underestimated, and a stiffer storey being predicted.

### 3.2 Case study

One of the motivations of this project was to investigate potential limitations with the current New Zealand loading standard (NZS1170.5:2004) in terms of predicting the deformation demands on EBF structures subject to earthquake loading. To evaluate whether the code is providing a reliable estimation of the link rotation demands, an 8-storey EBF case study structure was selected. This proposed structure was designed by HERA (Clifton and Cowie, 2013) based on the current NZS 1170.5:2004 code requirements.

#### 3.2.1 Assessing the link rotation demand - HERA

Following the design example provided by HERA, the design ductility $\mu$ was set at 4 for this case study structure, with a design base shear $V$ of 1000 kN. Since it was an 8-storey building, the deflection scale factor $k_d$ was set to 0.85 according to NZS1170.5:2004. The total height of the structure was 29 m. The rooftop displacement, $\Delta_B$, was obtained from the lateral load analysis as 46 mm. Therefore, the ultimate storey drift, $\theta_p$, was calculated to be 0.004 rad using Equation 1.

In the current code approach recommended by Clifton and Cowie (2013), the storey drift was assumed to be the same for all levels. The inelastic rotation angle between the active link and adjacent beam, $\gamma_p$, was calculated using Equation 2 to be 0.06 rad for the case sturdy structure, which was the same for all levels.

The rooftop displacement that could be expected at the ultimate limit state was calculated to be 0.1173 m by multiplying the ultimate drift angle using the total height. To permit a consistent comparison with other
analysis methods, this rooftop displacement value was also used in the Ruaumoko pushover analysis and the
demformation components method prediction as a target displacement at ULS.

3.2.2 Assessing the link rotation demand - Ruaumoko

A corresponding Ruaumoko model of the proposed 8-storey EBF structure was created to study the real
deformation behaviour of the structure. The model was analysed using inelastic pushover analysis, with an
output file produced at the ELS and ULS.

The drift values at each level were extracted from the output file. The link rotations at each level, $\gamma_{RMK,link,i}$,
were calculated by extracting the vertical displacements of the two end nodes of the link and dividing their
sum by the original link length.

3.2.3 Assessing the link rotation demand – Deformation Components Method

The deformation demands at ELS and ULS were also assessed using the deformation components method.
The displacement profile at ELS was plotted against the one obtained from Ruaumoko, as shown in Figure 6.

It was found that the link on ground level yielded first at a base shear of 1221 kN. The maximum difference
between the prediction and the Ruaumoko analysis result regarding the displacement at each storey was
14.9% and 60.4% in terms of storey drifts.

The ULS displacement profile was produced by uniformly scaling the ELS displacement profile until a
rooftop displacement of 0.1137 m was achieved. It was plotted against the HERA calculation and the
Ruaumoko analysis result, as shown in Figure 7.

The displacement profile obtained from the deformation components method and the Ruaumoko analysis
matched well, with a maximum difference of 9.72% appeared at the first storey. The post-yield link
component of the storey drift was calculated using Equation 17, assuming that all post-yield deformation
concentrated at the link. Figure 8 demonstrates how the different components vary with the increase in the
storey drift for Level 5 in the proposed structure.

The link rotations at each level, $\gamma_{DC,link,i}$, at ULS were calculated using Equation 18 and Equation 19. They
were compared with the results obtained from Ruaumoko analysis and HERA’s prediction. The percentage
difference between $\gamma_{DC,link,i}$ and $\gamma_{RMK,link,i}$ were also calculated. These results are summarised in Table 2.
3.2.4 Limitations with current guidelines

In the design example provided by HERA, the inelastic link rotation angle between the active link and the adjacent beam should be less than 0.08 rad. The maximum possible link rotation in the proposed structure was calculated to be 0.06 rad using HERA’s method (Clifton and Cowie, 2013), which stayed within the safe range. However, the inelastic pushover analysis results obtained from Ruaumoko indicated that the maximum link rotation was 0.066 rad, which exceeded the HERA approach by 10%. This suggested that the current code provisions underestimated the actual link rotations of the EBF structures. This could lead to the members being designed with insufficient deformation capacity under earthquake loading. The results also indicated that the link rotation demands vary significantly between different stories, which was not captured in the current code approach.

By applying the deformation components method, the maximum link rotation was predicted to be 0.071 rad, which agreed closely with the inelastic pushover analysis results obtained from Ruaumoko with a 7% error. Therefore, the deformation components method provided a more accurate and conservative prediction of the inelastic link rotation demand for the proposed 8-storey EBF structure and can be used to replace the results obtained from inelastic pushover analysis at preliminary design stage.

3.3 One storey coupled EBF structure

It could be seen from above that the current code has certain limitations on assessing the deformation of EBF systems under lateral loads. Moreover, it did not specify any guidelines for assessing the deformation of coupled EBF structures. The deformation components method, however, is theoretically able to predict the displacement and link rotation demand for such structures. Figure 9 shows a one storey coupled EBF structure, which was proposed to investigate the behaviour of such structures under increased storey drift. By adjusting the link lengths, the two EBFs in this structure were set to provide the same initial stiffness with different sections. The whole structure was pushed with a storey drift 0.3%, which saw both links yield. The link components of the storey drift are plotted with the total storey drift, as shown in Figure 10. The displacement ductility demand on the two links can be calculated using Equation 20.

\[
\mu_{d,\text{link},i} = \frac{\theta_{u,\text{link},i}}{\theta_{y,\text{link},i}}
\]
At a storey drift level of 0.3%, the displacement ductility was calculated to be 6.3 for Link 1, and 9.6 for Link 2. They were designed with the same initial stiffness, but their ductility demands differed by more than 30% at the target post-yield drift. This could potentially create a critical difference in the detailing of this type of coupled EBF structures, which requires more study on their deformation behaviours based on the deformation components method.

4 CONCLUSIONS AND RECOMMENDATIONS

This study shows that the current New Zealand loading standard, NZS 1170.5:2004, could underestimate the deformation demands of EBF structures, especially the link rotation relative to the beam, under earthquake loading. The actual displacement profile and link rotation demands found by conducting advanced non-linear pushover analysis using Ruaumoko could be well represented by the proposed deformation components method.

The deformation components method can predict the displacement profile of EBF structures for both the elastic limit state and the ultimate limit state, at a target displacement or a storey drift value, with relatively high accuracy. However, it appears to have limited accuracy in predicting storey drift demands for mid-rise and high-rise EBF structures. Discrepancies were found to be from deformations associated with column axial forces and brace joint displacements.

A major limitation in the current code approach for EBF structures appears to be the assumption that the structure has a constant storey drift for all levels at the ultimate limit state and the post-yield deformation is shared by all components. However, the actual storey drift varies significantly between different stories and most of the post-yield deformation in one storey is taken by the link rotation. Therefore, it is suggested that application of the displacement components method at a preliminary design stage would help identify the actual deformation requirements for links.

REFERENCES


